

# 2D Geometry Formulas

## Area Formulas

Area of a square:  $A = s^2$

Area of a rectangle:  $A = l \cdot w$

Area of a triangle:  $A = \frac{1}{2} \cdot b \cdot h$

Area of a parallelogram:  $A = b \cdot h$

Area of a circle:  $A = \pi r^2$

$s$  = Side of the Square  
 $l$  = length of the rectangle

## Perimeter Formulas

Perimeter of a square:  $P = 4s$

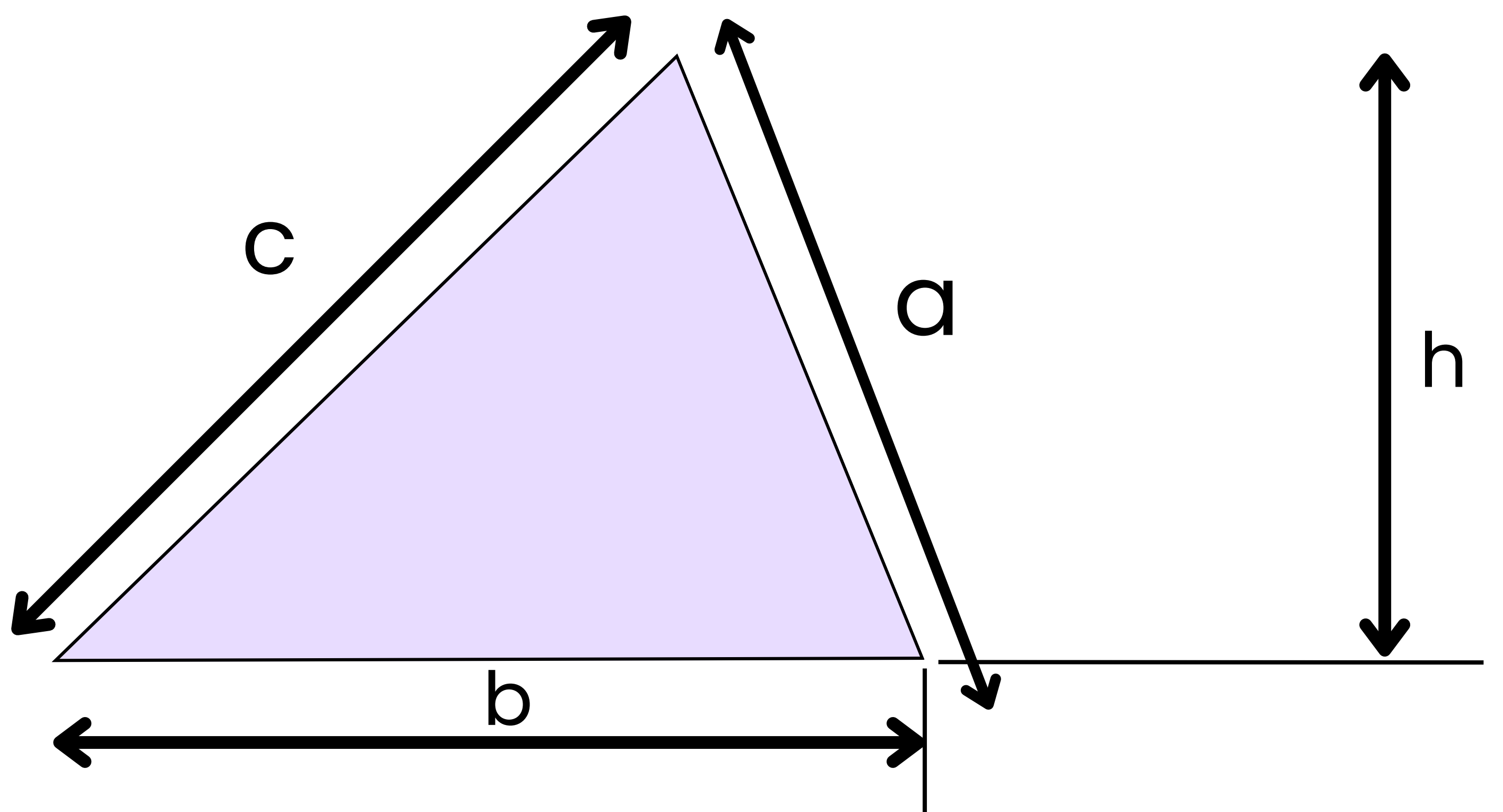
Perimeter of a rectangle:  $P = 2(l + w)$

Perimeter of a triangle:  $P = a + b + c$

Perimeter (circumference) of a circle:  $C = 2\pi r$

# Triangle Formulas

a, b, and c are the lengths of the sides).



## Area Formulas

**Standard Area Formula:**

$$\text{Area} = \frac{1}{2} \times \text{base} \times \text{height}$$

**Heron's Formula :**

$$s = \frac{a+b+c}{2} \quad (\text{for sides } a, b, c \text{ and semi-perimeter } s):$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

**Area of an Equilateral Triangle:**

$$\text{Area} = \frac{\sqrt{3}}{4} \times a^2 \quad (\text{where } a \text{ is the length of a side}).$$

# Triangle Formulas

## Perimeter Formulas

**Standard Area Formula:**

$$\text{Area} = \frac{1}{2} \times \text{base} \times \text{height}$$

**Heron's Formula :**

$$s = \frac{a+b+c}{2} \quad (\text{for sides } a, b, c \text{ and semi-perimeter } s):$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

**Area of an Equilateral Triangle:**

$$\text{Area} = \frac{\sqrt{3}}{4} \times a^2 \quad (\text{where } a \text{ is the length of a side}).$$

## Perimeter Formulas

**Length of Median**

$$m_a = \sqrt{\frac{2b^2 + 2c^2 - a^2}{4}}$$

# Triangle Formulas

## Perimeter Formulas

### Altitude

$$h = \frac{2 \times \text{Area}}{\text{base}} \quad (\text{perpendicular segment from a vertex to the line containing the opposite side):$$

### Angle Bisector

$$l_a = \sqrt{bc \left(1 - \frac{a^2}{(b+c)^2}\right)} \quad (\text{line segment that splits an angle into two equal angles})$$

## Circle Formulas Related to Triangles

### Circumradius

$$R = \frac{abc}{4 \times \text{Area}} \quad (\text{radius of the circumscribed circle}):$$

### Inradius

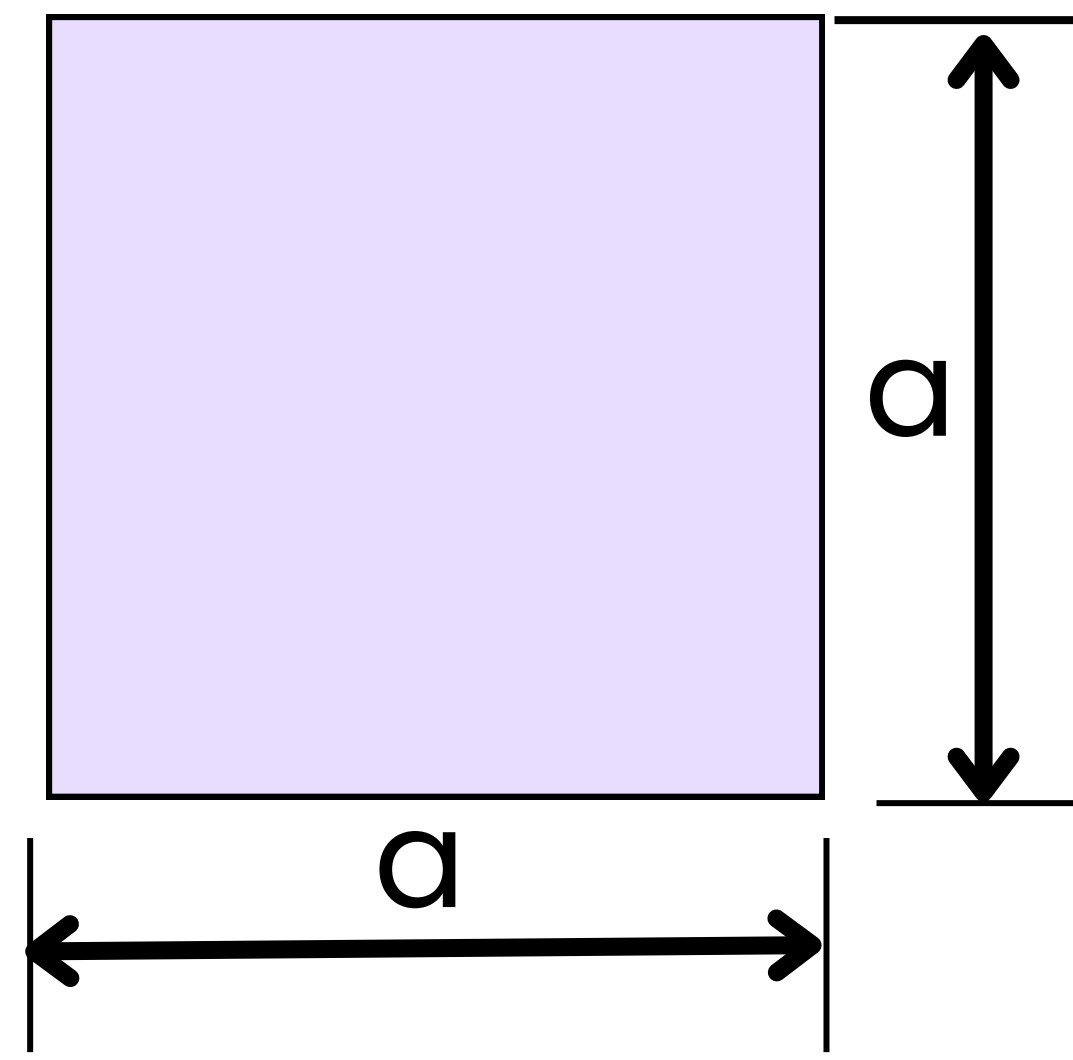
$$r = \frac{\text{Area}}{s} \quad (\text{radius of the inscribed circle}):$$

### Exradius

$$r_a = \frac{\text{Area}}{s-a} \quad (\text{radius of the excircle opposite side } a):$$

# Square Formulas

( $a$  is the lengths of the sides).



## Area of a Square

$$A = a^2$$

The area ( $A$ ) of a square is the space contained within its four sides.

## Perimeter of a Square

$$P = 4a$$

( $a$  = length of one side of the square)  
The perimeter ( $P$ ) of a square is the total distance around the outside of the square.

## Diagonal of a Square

$$d = a\sqrt{2}$$

( $a$  = length of one side of the square)  
The diagonal ( $d$ ) of a square is the line segment connecting two opposite corners.

## Circumcircle of a Square

$$R = \frac{a\sqrt{2}}{2} = \frac{d}{2}$$
 (The circumcircle is a circle that passes through all four vertices of the square.)

## Incircle of a Square

$$r = \frac{a}{2}$$

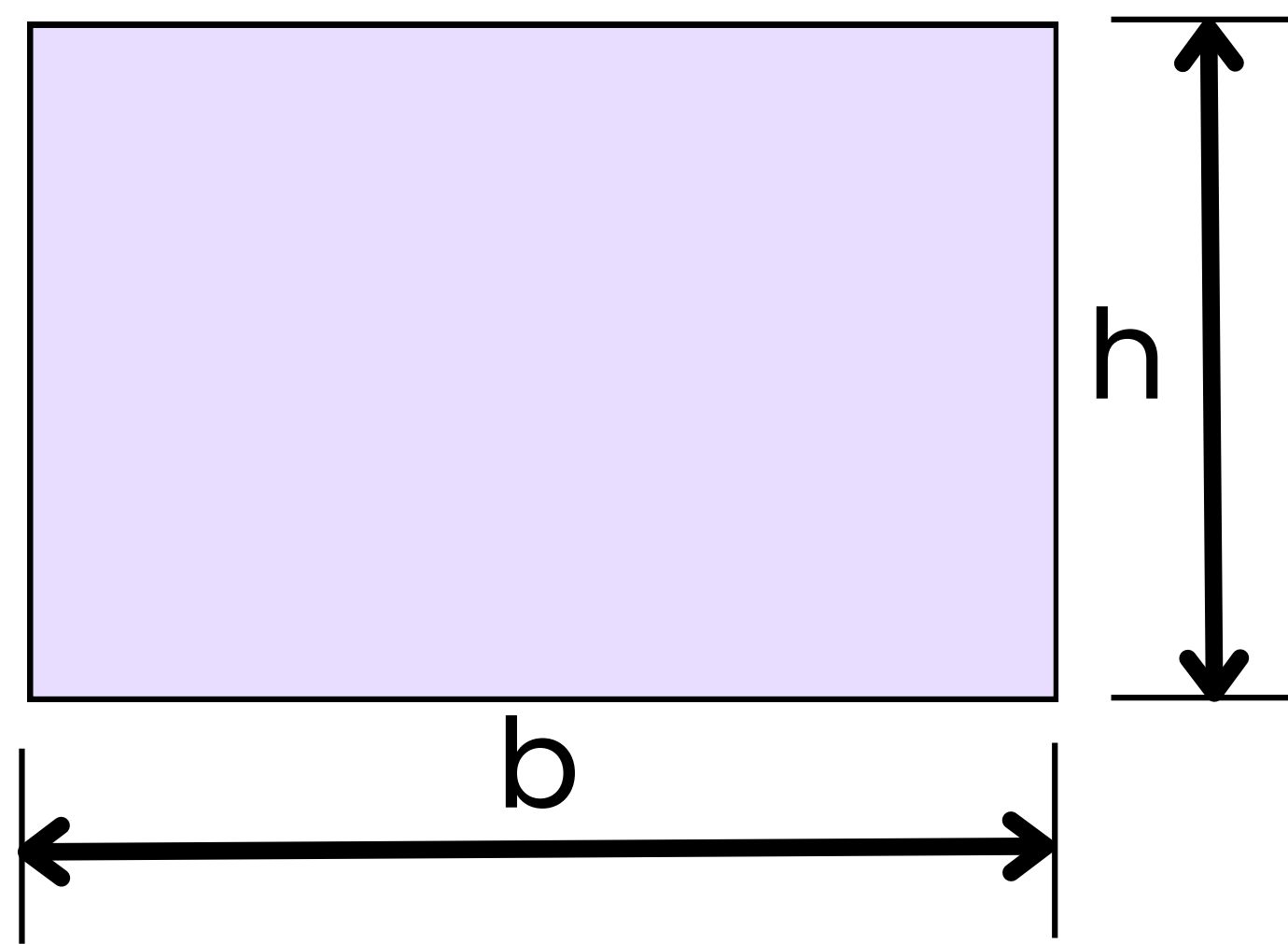
(The incircle is a circle that is tangent to all four sides of the square.)

## Relationship Between Diagonal and Side Length

$$a = \frac{d}{\sqrt{2}}$$

If the diagonal ( $d$ ) is known, the side length( $a$ )

# Rectangle Formulas



## Area

$$\text{Area} = \text{Length} \times \text{Width}$$

(The area of a rectangle is the amount of space enclosed within its sides.)

## Perimeter

$$\text{Perimeter} = 2 \times (\text{Length} + \text{Width})$$

(The area of a rectangle is the amount of space enclosed within its sides.)

## Diagonal of a rectangle

$$\text{Diagonal} = \sqrt{(\text{Length}^2 + \text{Width}^2)}$$

(The diagonal of a rectangle is the line segment connecting two opposite corners. It can be calculated using the Pythagorean theorem.)

## Length (Given Area and Width)

$$\text{Length} = \frac{\text{Area}}{\text{Width}}$$

(If you know the area and width, you can find the length.)

## Length (Given Perimeter and Width)

$$\text{Width} = \frac{\text{Area}}{\text{Length}}$$

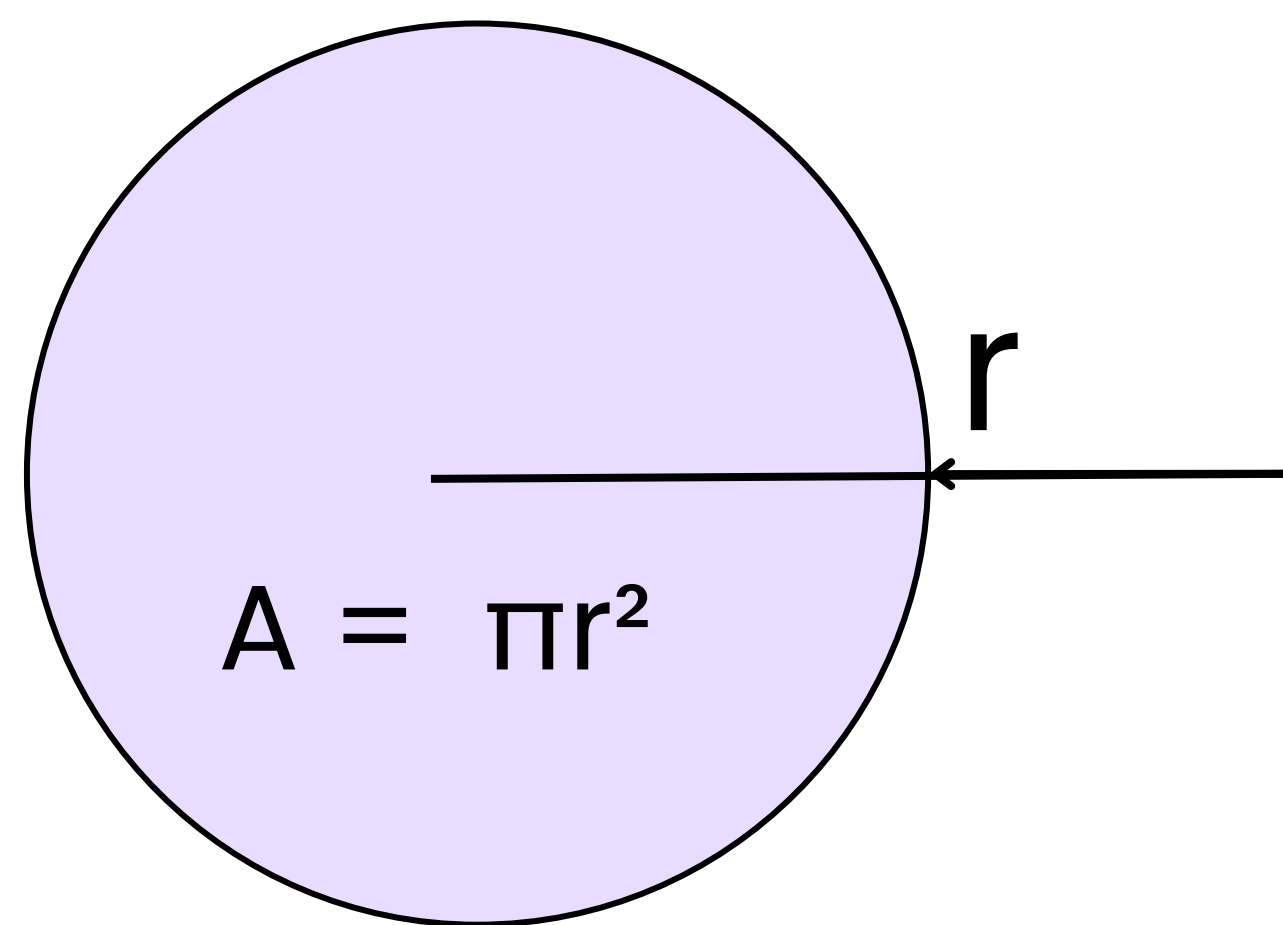
(If you know the area and length, you can find the width.)

## Width (Given Perimeter and Length)

$$\text{Length} = \frac{\text{Perimeter}}{2} - \text{Width}$$

(If you know the perimeter and width, you can find the length)

# Circle Formulas



## Circumference

$$C = 2\pi r$$

C: Circumference

r: Radius

$\pi$  (pi): Approximately 3.14159

## Area

$$A = \pi r^2$$

A: Area

r: Radius

$\pi$  (pi): Approximately 3.14159

## Diameter

$$D = 2r$$

The diameter is the distance across the circle, passing through the center. It is twice the radius.

D: Diameter

r: Radius

## Radius

$$r = \frac{D}{2}$$

The radius is the distance from the center of the circle to any point on its circumference.

D: Diameter

r: Radius

## Equation of a Circle (Standard Form)

$$(x - h)^2 + (y - k)^2 = r^2$$

The standard form equation of a circle with its center at (h,k) and radius r is:

(h,k): Coordinates of the center

(x,y): Coordinates of any point on the circle

## Equation of a Circle (General Form)

$$x^2 + y^2 + Dx + Ey + F = 0$$

D, E, F: Constants

To convert from the standard form to the general form, expand and rearrange the standard form equation.