

AP Physics C: Electricity & Magnetism 2000 Scoring Guidelines

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E&M. 1 (15 points)

(a) 4 points

Since brightness is proportional to the power dissipated by a bulb, the answer may be found by solving the circuit to determine the power dissipated by each bulb. For example,

$$\frac{1}{R_p} = \frac{1}{12 \Omega} + \frac{1}{6 \Omega} = \frac{3}{12 \Omega}$$
, where R_p is the resistance of the parallel combination of resistors

$$R_p = 4\Omega$$

$$I_A = \frac{\mathcal{E}}{R_A + R_p} = \frac{42 \text{ V}}{10 \Omega + 4 \Omega} = 3 \text{ A}$$

$$I_B = \frac{V_p}{R_B} = \frac{I_A R_p}{R_B} = \frac{(3 \text{ A})(4 \Omega)}{12 \Omega} = 1 \text{ A}$$

$$I_C = \frac{V_p}{R_C} = \frac{I_A R_p}{R_C} = \frac{3 \cdot 4(3 \text{ A})(4 \Omega)}{6 \Omega} = 2 \text{ A}$$

$$P_A = I_A^2 R_A = (3 \text{ A})^2 (10 \Omega) = 90 \text{ W}$$

• •
$$P_B = I_B^2 R_B = (1 \text{ A})^2 (12 \Omega) = 12 \text{ W}$$

$$P_C = I_C^2 R_C = (2 \text{ A})^2 (6 \Omega) = 24 \text{ W}$$

For correct ordering, i.e., bulb A is brighter than bulb C, which is brighter than bulb B (Partial credit of 1 point given for incorrect answer but with an indication that bulb A is brightest or that bulb C is brighter than bulb B.)

For a correct explanation, which can be by a quantitative solution for the currents and powers as above, or by a qualitative approach that notes that all the current in the circuit flows through bulb A, then branches in such a way that bulb C receives more current than bulb B.

3 points

1 point

(b)

3 points

Immediately after the switch is closed there is no current in the inductor so the circuit consists of resistors A and B in series with the source of emf.

For
$$I_C = 0$$
For recognition that $I_A = I_B$ and they are nonzero

1 point

1 point

2 point

2 point

3 point

4 point

4 point

4 point

1 point

1 point

1 point

Distribution of points

E&M. 1 (continued)

(b) (continued)

ii. 3 points

A long time after the switch is closed, the potential difference across the inductor is zero, so the circuit is essentially the same as in part (a)

For recognizing that $V_L = 0$

For correct currents, the same as in part (a), i.e., $I_A = 3$ A, $I_B = 1$ A, I = 2 A

(If currents not computed in part (a), they could be computed here.)

Unit point: For expressing all currents in (b) in correct units of amperes

1 point

1 point

2 points

(c) 2 points



Attributes of correct curve:

- 1. Starts at a nonzero but finite point on the vertical axis
- 2. Smooth
- 3. Concave upward
- Has asymptote equal to zero

For a correct curve with all four attributes

2 points

Partial credit of 1 point for curve with flaws but at least two correct attributes

E&M. 1 (continued)

(d) 2 points



Attributes of correct curve:

- 1. Starts at zero
- 2. Smooth
- 3. Concave downward
- 4. Has finite but nonzero asymptote
- For a correct curve with all four attributes

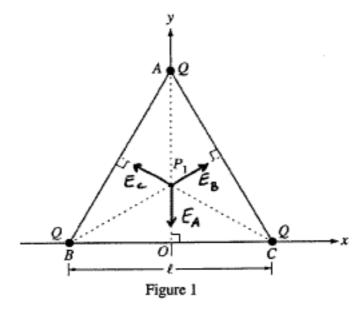
2 points

Partial credit of 1 point for curve with flaws but at least two correct attributes

E&M. 2 (15 points)

(a)

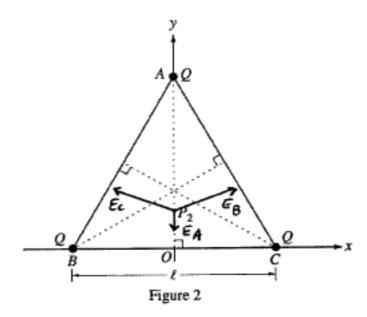
i. 6 points



• . One point for each arrow drawn in the correct direction

3 points

For not having all arrows approximately the same length, deduction of 1 point For not having all arrows start at P_1 , deduction of 1 point For having one or more extra vectors, deduction of 1 point



One point for each arrow drawn in the correct direction

3 points

For not having lengths of arrows such that $E_C \approx E_B > E_A$, deduction of 1 point For not having all arrows start at P_2 , deduction of 1 point For having one or more extra vectors, deduction of 1 point

E&M. 2 (continued)

- (a) (continued)
 - ii. 3 points

	Greater than at P ₁	Less than at P ₁	The same as at P_1
E_A		~	
$E_{\mathcal{B}}$	V		
E_C	· /		

One point for having check mark or other indicator in each correct box

3 points

- (b) 1 point
- For an indication that the x-components of the field vectors due to particles C and B cancel each other due to the symmetry created by having a vertex of the triangle on the y-axis

1 point

(c) 3 points

For an indication that the potential is the sum of the potentials due to the individual

1 point

 $V = \sum_{i} \frac{kQ_{i}}{r_{i}} = k \left(\frac{Q_{A}}{r_{A}} + \frac{Q_{B}}{r_{B}} + \frac{Q_{C}}{r_{C}} \right)$

For recognition that the terms due to the particles at B and C are equal

1 point

$$V = k \left(\frac{\bar{Q}_A}{r_A} + \frac{2Q}{r_B} \right)$$

For correct substitutions for Q's and r's and correct answer

$$V = \frac{1}{4\pi\epsilon_0} \left(\frac{Q}{\frac{\sqrt{3}\ell}{2} - y} + \frac{2Q}{\sqrt{\frac{\ell^2}{4} + y^2}} \right), \text{ or equivalent}$$

Distribution of points

E&M. 2 (continued)

(d) 2 points

Since $E_y = -\frac{d}{dy}V(y)$, to find the y coordinates of the points on the y-axis at which the electric field is zero, take the derivative of the expression in part (c) with

the electric field is zero, take the derivative of the expression in part (c) with respect to y, set the expression equal to zero and solve for y.

For recognition that E is a derivative of V

For recognition that $\frac{dV}{dy} = 0$

1 point

Distribution of points

E&M. 3 (15 points)

(a)

3 points

For a correct statement of Gauss's law

1 point

$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon}$$

For expressing the permittivity of the oil in terms of the dielectric constant κ

1 point

$$\epsilon = \kappa \dot{\epsilon}_0$$

For a correct expression for the electric field in the oil

1 point

$$E(2\pi rL) = \frac{Q}{\kappa \epsilon_0}$$

$$E = \frac{Q}{2\pi\kappa\epsilon_0 rL}$$

ii. 2 points

For a correct statement of Gauss's law in the space outside the outer shell

1 point

For stating that the electric field is zero in this region

1 point

$$\mathbf{E} = 0$$

(b)

i. 3 points

For an expression for the electric potential between the two shells

1 point

$$\Delta V = V_b - V_a = \int_a^b E_r dr$$

For substituting the expression for the electric field between the shells $\Delta V = \frac{Q}{2\pi\kappa\epsilon_0 L} \int_a^b \frac{dr}{r}$

1 point

$$\Delta V = \frac{Q}{2\pi\kappa\epsilon_0 L} \int_a^b \frac{dr}{r}$$

For a correct expression for the electric potential difference between the shells

$$\Delta V = \frac{Q}{2\pi\kappa\epsilon_0 L} \ln\left(\frac{b}{a}\right)$$

Distribution of points

E&M. 3 (continued)

- (b) (continued)
 - ii. 2 points

For an expression for the capacitance in terms of Q and ΔV

1 point

$$C = \frac{Q}{\Delta V}$$

Substituting the expression for ΔV from (b)i:

$$C = \frac{Q}{\frac{Q}{2\pi\kappa\epsilon_0 L} \ln\left(\frac{b}{a}\right)}$$

For a correct expression for the capacitance

1 point

$$C = \frac{2\pi\kappa\epsilon_0 L}{\ln\left(\frac{b}{a}\right)}$$

(c) ?

3 points i.

For a correct statement of Ampere's law

1 point

$$\oint \mathbf{B} \cdot d\boldsymbol{\ell} = \mu_0 I$$

For substituting the current through the inner shell $B(2\pi r) = \mu_0 \left(\frac{\mathcal{E}}{R}\right)$

1 point

$$B(2\pi r) = \mu_0 \left(\frac{\mathcal{E}}{R}\right)$$

For a correct expression for the magnetic field between the shells

1 point

$$B = \frac{\mu_0 \mathcal{E}}{2\pi r R}$$

ii. 2 points

For the correct substitution of the total current through both shells in to Ampere's law

1 point

$$B(2\pi r) = \mu_0 \left(\frac{4\mathcal{E}}{R}\right)$$

For a correct expression for the magnetic field around the outer shell

$$B = \frac{2\mu_0 \mathcal{E}}{\pi r R}$$