

AP® Calculus AB 2004 Sample Student Responses Form B

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t (minutes)	0	5	10	15	20	25	30	35	40
v(t) (miles per minute)	7.0	9.2	9.5	7.0	4.5	2.4	2.4	4.3	7.3

Work for problem 3(a)

$$UYECL = 10(f(5) + f(15) + f(25) + f(35)$$

$$= 10(9.2 + 7 + 2.4 + 4.3)$$

area = 229 miles

 $5_0^{40}v(t)dt$ 15 the total distance traveled between t=0 and t=40 minutes

Work for problem 3(b)

a(£)=0

between ())

on the intervals [0,15] and [25,30]

the Smallest humber of instances the acceleration can equal zero is 2 by MUT and Rolle's Theorem

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Work for problem 3(c)

$$f'(t) = \frac{1}{10} \sin^{4} |_{10} + 3.7 \cos^{74} |_{40}$$

 $f'(t) = -\frac{1}{10} \sin^{4} |_{10} + 21 |_{40} \cos^{74} |_{40}$
 $f'(23) = -\frac{1}{10} \sin^{23} |_{10} + \frac{21}{40} \cos^{16} |_{40}$
 $f'(23) = -\frac{408 \text{ miles per minute}^{2}}{10}$

Work for problem 3(d)

 $\frac{1}{40-0}$ $\int_{0}^{40} 6 + \cos(4/10) + 3\sin(74/40) d4$

average velocity = 40.236.65079

= 5.916 miles per minute

END OF PART A OF SECTION II

IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON PART A ONLY. DO NOT GO ON TO PART B UNTIL YOU ARE TOLD TO DO SO.

t (minutes)	0	5	10	15	20	25	30	35	40
v(t) (miles per minute)	7.0	9.2	9.5	7.0	4.5	2.4	2.4	4.3	7.3

Work for problem 3(a)

$$\int_{0}^{40} v(t) dt = \frac{40-0}{4} \left[9.2 + 7 + 2.4 + 4.3 \right]$$

$$= \frac{40}{4} \left[22.9 \right] = 229 \text{ miles}$$
distance plane flies.

Work for problem 3(b)

Acceleration of the plane equals a zero where the graph changes concavity. There are 2 such instances one at t=10min 4 the other $t\in(25,30)$.

$$a(t) = \frac{df}{dt} = \frac{-1}{10} \sin\left(\frac{t}{10}\right) + \frac{21}{40} \cos\left(\frac{7t}{40}\right)$$

$$a(23) = \frac{-1}{10} \sin(2.3) + \frac{21}{40} \cos\left(\frac{161}{40}\right) \approx -0.408 \text{ miles/min}^2.$$

Work for problem 3(d)

and velocity =
$$\frac{1}{40-0} \int_{0}^{40} f(t) dt = \frac{1}{40} \int_{0}^{40} 6 + \omega s(\frac{t}{10}) + 3 \sin(\frac{7t}{40})$$

$$= \frac{1}{40} \left[6t + 10 \sin(\frac{t}{10}) - 3 \cos(\frac{7t}{40}) (\frac{40}{7}) \right]_{0}^{40}$$

$$= \frac{1}{40} \left[6t + 10 \sin(\frac{t}{10}) - \frac{120}{7} \cos(\frac{7t}{40}) \right]_{0}^{40}$$

$$= \frac{1}{40} \left[240 - 7.568 - 12.924 - (-\frac{120}{7}) \right]$$

$$= 5.916 \frac{\text{miles}}{\text{min}}$$

END OF PART A OF SECTION II

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