

AP Calculus BC 2000 Student Samples

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Work for problem 5(a)

(a)
$$xy^{2} - x^{3}y = C$$

 $x(2y)(3x) + y^{2} - 3x^{2}y - x^{3}(3x) = 0$
 $(3x)(3x) + y^{2} - 3x^{2}y - y^{2}$
 $(3x)(3x) + y^{2} - 3x^{2}y - y^{2}$

Work for problem 5(b)

$$(1)y^{3} - (1)y = 6$$

$$y^{2} - y - 6 = 0$$

$$(y + a)(y - 3) = 0 \qquad (1, -a) \text{ and } (1, 3)$$

$$x = -2 \text{ or } 3$$

$$\frac{dy}{dx}|_{(1, -a)} = \frac{3(1)(-a) - 4}{2(-a)(1) - (1)} = \frac{-6 - 4}{-4 - 1} = \frac{-10}{-5} = 2$$

$$x = 2(x - 1) - 2$$

$$x = 2(x - 1) - 2$$

$$x = 2(x - 1) - 2$$

$$x = 3(x - 1) - 3$$

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Work for problem 5(c)

when
$$2xy-x^3=0$$

$$x = 0 \text{ or } 3y = x^{3}$$

$$x = 0 \text{ or } 3y - x^{3} = 0$$

$$x = 0 \text{ or } 3y - x^{3} = 0$$

$$(0)y-(0)y=6$$

0 \(\psi \)

Work for problem 5(a)

$$xy^{2} - (x^{3}y) = 6$$

$$(x \cdot 2yy') + (y^{2}) - (x^{3}y') + (3x^{2}y \cdot) = 0$$

$$2xyy' + y^{2} - x^{3}y' - 3x^{2}y = 0$$

$$2 \times yy' - x^3y' = 3 \times ^2y - y^2$$

$$y'(2 \times y - x^3) = 3 \times ^2y - y^2$$

$$y' = 3 \times ^2y - y^2$$

$$2 \times y - x^3$$

Work for problem 5(b)

$$xy^2 - x^3y = 6$$

 $(1)y^2 - (1)^3y = 6$
 $y^2 - y = 6$
 $y^2 - y - 6 = 0$
 $(y - 3)xy + 2)$
 $y = 3 - 2$

$$m = 3(1)^{2}(3) - (3)^{2}$$

 $m = 3(1)^{2}(3) - (3)^{2}$

x = 1

$$M = \frac{3x^2y - y^2}{2xy - x^3}$$

$$M = \frac{3(1)^2(-2) - (-2)^2}{2(1)(-2) - (1)^3}$$

= -6-4 : -16 :

Continue problem 5 on page 13.

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5 5 5 5 5 5 5 5 5 C₁

Work for problem 5(c)

tangent line = vertical when denominator of dr is a

50 0 = 2 × y - ×3

Work for problem 5(a)

$$xy^{3}-x^{3}y=6$$

 $x \cdot 2y + y^{2} - x^{3} + y(-3x^{3})=0$
 $2xy + + y(-3x^{3})=0$

Work for problem 5(b)

$$(1)y^{2} - (1)^{3}y = 6$$

$$y^{2} - y = 6$$

$$y^{2} - y - 6 = 0$$

$$1 = \sqrt{-1^{2} - 4(1)(-6)}$$

$$1 = \sqrt{25}$$

$$(1,6) \text{ and } (1,-4)$$

$$1 + 5 \text{ or } 1-5$$

$$6 \text{ or } -4$$

r problem 5(b)
$$y = 6 = -\frac{18}{11}(x-1)$$

$$y = -\frac{18}{11}(x-1) + 6$$

$$y^{2} - y = 6$$

$$y^{2} - y = 6$$

$$y^{2} - y = 6$$

$$y = -\frac{12}{11}(x-1) + 6$$

$$\frac{3x^{2}y^{2}y^{2}}{2xy^{2} - x^{3}} = \frac{dy}{dx}$$

$$\frac{3(1)^{2}y^{2} - y^{2}}{2(1)(1)^{2}y^{2}} = \frac{12 - 16}{8 - 1} = -\frac{14}{7}$$

$$\frac{3(1)^{2}y^{2} - y^{2}}{2(1)(1)^{2}y^{2}} = \frac{12 - 16}{8 - 1} = -\frac{14}{7}$$

$$\frac{y - 4 = -\frac{14}{7}(x - 1) + y^{2}}{y^{2}} = \frac{12 - 16}{8 - 1} = -\frac{14}{7}$$

$$y - 4 = -\frac{14}{7}(x - 1) + y^{2}$$

$$y - 4 = -\frac{14}{7}(x - 1) + y^{2}$$

$$y - 4 = -\frac{14}{7}(x - 1) + y^{2}$$

Continue problem 5 on page 13.

Work for problem 5(c)

$$2xy - x^{3} = 0$$

$$2x(-\frac{1}{7}(x-1)+4) - x^{3} = 0$$

$$-\frac{1}{7}x^{2} + \frac{1}{7}x + 4)$$

$$-\frac{1}{7}x^{2} + \frac{1}{7}x + 4)$$

$$-\frac{1}{7}x^{2} + \frac{1}{7}x + \frac{1}{7}x = 0$$

$$-\frac{1}{7}x^{2} + \frac{1}{7}x = 0$$

$$\frac{1}{7}x + \frac{1}{7}x = 0$$

$$\frac{1}{7}x + \frac{1}{7}x = 0$$

$$\frac{1}{7}x + \frac{1}{7}x = 0$$