### **Question 2**

### Intent of Question

The primary goals of this question were to assess a student's ability to (1) identify, set up, perform, and interpret the results of an appropriate hypothesis test to address a particular question and (2) assess the effectiveness of treatments in a controlled experiment.

### <u>Solution</u>

#### Part (a):

Step 1: States a correct pair of hypotheses.

- ${\rm H}_{\rm 0}$  : The proportion of children who would choose each snack is the same regardless of which type of ad is viewed.
- ${\rm H}_{\rm a}$  : The proportion of children who would choose each snack differs based on which type of ad is viewed.

Step 2: Identifies a correct test procedure (by name or formula) and checks appropriate conditions.

The appropriate procedure is a chi-square test of homogeneity.

The conditions for this test are satisfied because (1) the question states that the children were randomly assigned to groups, and (2) expected counts for the six cells of the table are all at least 5, as seen in the following table that lists expected counts beside observed counts.

Group	Choco-Zuties	Apple-Zuties	Total
А	21 (18.67)	4 (6.33)	25
В	13 (18.67)	12 (6.33)	25
С	22 (18.67)	3 (6.33)	25
Total	56	19	75

Step 3: Calculates the appropriate test statistic and *p*-value.

The test statistic is calculated as  $\chi^2 = \sum \frac{(O-E)^2}{E}$ , which is

$$\chi^2 \approx$$
  
0.292 + 0.860 +  
1.720 + 5.070 +  
0.595 + 1.754  $\approx$  10.291

The *p*-value is  $P(\chi^2_{df2} \ge 10.291) \approx 0.006$ .

Step 4: States a correct conclusion in the context of the study, using the result of the statistical test.

Because the *p*-value is very small (for instance, much smaller than  $\alpha = 0.05$ ), we reject the null hypothesis at the 0.05 level (and at the 0.01 level). The data provide convincing statistical evidence that the proportions who would choose each snack differ based on which ad is viewed.

## **Question 2 (continued)**

### Part (b):

When neither ad was viewed,  $\frac{22}{25}$  or 88 percent of the children chose Choco-Zuties whereas only 12 percent chose Apple-Zuties.

When the Choco-Zuties ad was viewed, 84 percent of the children chose Choco-Zuties, which was very similar to the percentage that chose them without viewing any ad. So watching the Choco-Zuties ad did not affect the snack choice very much.

When the Apple-Zuties ad was viewed, only  $\frac{13}{25}$  or 52 percent of the children chose Choco-Zuties, and 48 percent chose Apple-Zuties. Watching the Apple-Zuties ad seemed to increase the proportion of children choosing Apple-Zuties.

#### <u>Scoring</u>

This question is scored in four sections. Section 1 consists of steps 1 and 2 in part (a); section 2 consists of step 3 in part (a); section 3 consists of step 4 in part (a); and section 4 consists of part (b). Sections 1, 2, 3 and 4 are scored as essentially correct (E), partially correct (P), or incorrect (I).

Section 1 is scored as follows:

Essentially correct (E) if the response includes the following three components:

- 1. Both hypotheses are stated correctly with at least one in context.
- 2. Identifies the correct test procedure (by name or by formula).
- 3. The technical conditions are checked (all expected counts are greater than or equal to 5).

Partially correct (P) if the response includes only two of the three components.

Incorrect (I) if the response correctly includes at most one of the three components.

Notes for component 1:

- It is acceptable if hypotheses are stated in terms of association/independence instead of proportions.
- Context must be included in at least one of the hypotheses, but is not required to be in both.
- If the hypotheses contain language that suggests that the response refers to the sample data, the component is not satisfied.

*Note for component 2*: It is acceptable if the test is identified as a test of independence instead of a test of homogeneity.

Notes for component 3:

- The random assignment condition was stated so need not be explicitly mentioned.
- Stating the expected count condition is met is not sufficient for component 3. The condition must be checked by reporting the expected counts and either:
  - o noting that all are greater than or equal to 5;

OR

## **Question 2 (continued)**

- o noting that all are greater than or equal to 1 and at most 20 percent are less than 5.
- Noting that the smallest expected count is 6.33 and that it is greater than or equal to 5 is sufficient to satisfy this component.
- Component 3 is not satisfied if the expected counts are reported as integers.
- This component is not satisfied if the response includes any of the following inappropriate conditions:
  - The response implies that a random sample was taken, e.g., "SRS check."
  - The response refers to independence of <u>groups</u> or independence of <u>ads</u> as a required condition.
  - The response indicates that a sample size greater than 30 ensures normality or the response implies normality as a condition.
- A response stating that <u>children</u> are independent can be ignored in the scoring of this component.

#### Section 2 is scored as follows:

Essentially correct (E) if the response includes the following three components:

- 1. Correct chi-square test-statistic
- 2. Correct degrees of freedom
- 3. Correct *p*-value

Partially correct (P) if the response includes only two of the three components.

Incorrect (I) if the response correctly includes at most one of the three components.

Notes:

- If the response makes an error in one calculation, future calculations are considered correct if they follow correctly from the initial miscalculation.
- A chi-square critical value approach is acceptable: The critical value for  $\alpha = 0.05$  is  $\chi^2 = 5.99$ .

#### **Section 3** is scored as follows:

Essentially correct (E) if the response provides a correct conclusion about the alternative hypothesis in context, *AND* provides justification based on linkage between the *p*-value and conclusion.

Partially correct (P) if the response provides a correct conclusion in context, but without justification based on linkage to the *p*-value;

OR

if the response provides a correct conclusion, with linkage to the p-value, but not in context; OR

if the response provides a correct decision stated in terms of the null hypothesis in context, with linkage to the *p*-value, but no conclusion is made about the alternative hypothesis.

Incorrect (I) if the response does not meet the criteria for E or P.

## **Question 2 (continued)**

#### Notes:

- If the conclusion is consistent with the *p*-value from section 2, and also in context with justification based on linkage to the *p*-value, section 3 is scored as E.
- If no alpha level is given, the solution must be explicit about the linkage by giving a correct interpretation of the *p*-value or by explaining how the conclusion follows from the *p*-value such as saying: "Because the *p*-value is small, we reject the null hypothesis." or "Because the *p*-value is large, we do not reject the null hypothesis."
- If a conclusion contains language that suggests that the response refers to the sample data, the conclusion component is not correct, unless the same error occurred in the statement of hypotheses in section 1.

#### **Section 4** is scored as follows:

Essentially correct (E) if the response, in context, concludes that ad type A had little effect and ad type B had an effect, both supported by the observed proportions (or counts) from the table.

Partially correct (P) if the response correctly concludes that ad type A had little effect, and ad type B had an effect but does not provide correct numerical justification;

OR

if the response compares all of the proportions (or counts) as required, but without correctly concluding ad effectiveness;

OR

if the response correctly describes the effect of one of the ad types A or B (in context, with correct numerical justification) but not the other;

OR

if the response compares all of the proportions (or counts) as required, but not in context.

Incorrect (I) if the response does not meet the criteria for E or P.

Each essentially correct (E) section counts as 1 point, and a partially correct (P) section counts as ½ point.

#### 4 Complete Response

- 3 Substantial Response
- 2 Developing Response
- 1 Minimal Response

If a response is between two scores (for example, 2½ points), use a holistic approach to decide whether to score up or down, depending on the strength of the response and communication.



Product advertisers studied the effects of television ads on children's choices for two new snacks. The
advertisers used two 30-second television ads in an experiment. One ad was for a new sugary snack called
Choco-Zuties, and the other ad was for a new healthy snack called Apple-Zuties.

For the experiment, 75 children were randomly assigned to one of three groups, A, B, or C. Each child individually watched a 30-minute television program that was interrupted for 5 minutes of advertising. The advertising was the same for each group with the following exceptions.

- The advertising for group A included the Choco-Zuties ad but not the Apple-Zuties ad.
- The advertising for group B included the Apple-Zuties ad but not the Choco-Zuties ad.
- The advertising for group C included neither the Choco-Zuties ad nor the Apple-Zuties ad.

After the program, the children were offered a choice between the two snacks. The table below summarizes their choices.

Group	Type of Ad	Number Who Chose Choco-Zuties	Number Who Chose Apple-Zuties		
Α.	Choco-Zuties only	21	4		
В	Apple-Zuties only	13	12 .		
С	Neither	22	3		

(a) Do the data provide convincing statistical evidence that there is an association between type of ad and children's choice of snack among all children similar to those who participated in the experiment?

Ho i	There.	is NO	Ô.	esociation	between	type	of	ad	and
	children's	choice	of	sNack.	8				

HA: There is an association between type of ad and

children's choice of snach.

 $\alpha = 0.05$ 

Conditions

- Reasonvable to assume that the 75 children are representative of all children similar to those who participated in the experiment.

- All expected counts are greater than 5 (see table), :

<u>Expected</u> counts A <u>Choco</u> <u>Apple</u> Since all conditions are met, 1 B <u>18.667</u> <u>6.333</u> will perform a chi-square test for C <u>18.667</u> <u>6.333</u> independence.

$$\chi^{2} = \frac{(21 - 18, 667)^{2}}{18, 6677} + \frac{(3 - 6333)^{2}}{6,333} = 10.2914$$

$$p(\chi^{2} > 10.2914) = 0.00582$$

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SF = 2

▶ If you need more room for your work in part (a), use the space below.

Since pea, we reject Ho, and find sufficient evidence to support the hypothesis that there is an association between type of ad and children's choice of snack

(b) Write a few sentences describing the effect of each ad on children's choice of snack. The choice - Zufies ad seemed to have little cheet on children's choice of snack. The children who watched the Choice - Zufies ad, Chose the sugary snack I less time that those who watched Neither ad, which is Not diverge. Significant.

The apple-Zuties ad had a much larger effect, of the children who watched the ad for Apple -Zuties, 10 more chose Apple-Zutiez than the children who watched weither ad

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choices.	,				
xp=total x total Grou		Type of Ad	Number Who Chose Choco-Zuties	Number Who Chose Apple-Zuties	Tota:
table	A	Choco-Zuties only	21 118.667	4 16.333	25
total	В	Apple-Zuties only	13 18.667	12 10.333	25
	С	Neither	22 118.667	3 6.333	25
children Ho: d:0.05 Hq:-	data provide a's choice of TMUU ad an TMSU ad and	mack among all children is no association d on it d Ken is an association childken is	vidence that there is an assument similar to those who pair clation between is choice of s ciation between distance of s	ticipated in the experiment of the type smarck en the type hack,	11? - 0{ 0{
1 will C	onduct	a chi Sq	uare test a	Associatio	rh
Condr	tions: (	Landom? 75	5 children vere	randomly as	signed

to one of those groups to one of those groups Independent? These ask at least 10(75)=750 childsen nationwide. Langelownts? All expected counts are greated than 5. (see chall above)

$$\chi^{2} = \sum_{i=1}^{7} \frac{(obs - exp)^{2}}{exp} = \frac{(21 - 18.667)^{2}}{18.667} + \frac{(4 - 6.333)^{2}}{6.333} = 10.29$$

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2B2 F2If you need more room for your work in part (a), use the space below.

Table C says the p-value Ranged from 0.01 to 0.005.

Since our p-value is less thom: our d of 0.05, I reject the null hypothesis. Those is convincing evidence that there is our association between the type of ad and duildrein's choice of snack.

(b) Write a few sentences describing the effect of each ad on children's choice of snack.

In group A, kids wore advertised Choico-Zuties and 84% of Them chose Choico-Zuties because of the ad. In group B, kids wore advertised Apple-Zuties and a significant increase was seen in mose who chose Apple-Zuties compared to group A. Almost 50% in Group B chose Apple-Zuties, thomas to The ad When Neither ad was shann, 88% chose chocozuties which show children's natural inclination towards sweets.

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Product advertisers studied the effects of television ads on children's choices for two new snacks. The advertisers used two 30-second television ads in an experiment. One ad was for a new sugary snack called Choco-Zuties, and the other ad was for a new healthy snack called Apple-Zuties.

For the experiment, 75 children were randomly assigned to one of three groups, A, B, or C. Each child individually watched a 30-minute television program that was interrupted for 5 minutes of advertising. The advertising was the same for each group with the following exceptions.

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- The advertising for group C included neither the Choco-Zuties ad nor the Apple-Zuties ad.

After the program, the children were offered a choice between the two snacks. The table below summarizes their choices.

Group	Type of Ad	Number Who Chose	Number Who Chose	
L	51	Choco-Zuties	Apple-Zuties	
А	Choco-Zuties only	21/18.67	4/ (0.3	
В	Apple-Zuties only	13/18.07	12/ 6.3	-
С	Neither	22 / 18.07	3/6-3	
		5(2	la	1

(a) Do the data provide convincing statistical evidence that there is an association between type of ad and children's choice of snack among all children similar to those who participated in the experiment?

HO! The null nepotheris is that x test of hamoyer ad hus no affect Smich Conditions: the children hander temattive hypothesis is Lide sende - add shown does have in cunatenacin the ) Kren nease. Let all that = , as Since D-vell 13 less than ox rejec al=,000 there is enough Saffe

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**262** of **2** If you need more room for your work in part (a), use the space below.

(b) Write a few sentences describing the effect of each ad on children's choice of snack.

According to the test there is evolup condence to suggest that the type atout the chirki Westerned has an effect on what shack they choose. However we still have to that mos account the Containing Variables. It is possible that seme Children just really like chocolote for example.

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# AP<sup>®</sup> STATISTICS 2016 SCORING COMMENTARY

### **Question 2**

#### Overview

The primary goals of this question were to assess a student's ability to (1) identify, set up, perform, and interpret the results of an appropriate hypothesis test to address a particular question and (2) assess the effectiveness of treatments in a controlled experiment.

#### Sample: 2A Score: 4

All three of the required components are present and correct for section 1. The response includes acceptable statements of hypotheses in terms of association between type of ad and children's choice of snack and indicates that a chi-square test for independence will be performed. A table of expected counts is provided, and a check that all are greater than 5 is made. The statement "Reasonable to assume that the 75 children are representative of all children similar to those who participated in the experiment" is considered extraneous. Section 1 was scored as essentially correct. All three of the required components are present and correct for section 2. The value of the chi-square statistic is correctly calculated, and the correct degrees of freedom and *p*-value are reported. (The *p*-value is identified by an acceptable probability statement.) Section 2 was scored as essentially correct. The statement  $p < \alpha$  establishes linkage between the previously calculated p-value and the chosen level of  $\alpha$  given in the response. A correct decision and a correct conclusion in context are provided. Section 3 was scored as essentially correct. In section 4 the response correctly states that the Choco-Zuties ad seemed to have little effect by noting that the difference between the number in the Choco-Zuties ad group and the number in the neither ad group is just one child. Establishing lack of ad effectiveness for group A because each group size is the same (25) is acceptable. By a similar argument, it is correctly stated that the Apple-Zuties ad had a much larger effect, noting that 10 more children in this group chose the Apple-Zuties snack than chose Apple-Zuties in the neither ad group. The value 10 here is incorrect; the correct value is 9. However, this is considered a minor arithmetic error that is overlooked. Thus the effectiveness of each type of ad is correctly addressed with numerical justification. Section 4 was scored as essentially correct. Because all four sections were scored as essentially correct, the response earned a score of 4.

#### Sample: 2B Score: 3

All three of the required components are present and correct for section 1. The response includes acceptable statements of hypotheses in terms of association and indicates that a chi-square test for association will be conducted. (The test is also correctly identified by formula). Correct expected counts are added to the table in the problem and noted as all being greater than 5. Though not required, the response also indicates that random assignment occurred. An additional condition labeled "Independent?" was considered extraneous information. Section 1 was scored as essentially correct. All three of the required components are present and correct for section 2. The value of the chi-square test statistic and the degrees of freedom are both correctly calculated. Correct upper and lower bounds on the *p*-value are obtained from Table C of the exam. Section 2 was scored as essentially correct. A correct conclusion is provided in context with justification based on linkage between the *p*-value and the chosen  $\alpha$  level given in the response. Section 3 was scored as essentially correct. In section 4 a comparison is made between group A (Choco-Zuties ad type) and group B (Apple-Zuties ad type), but this does not establish ad effectiveness or ineffectiveness. The response includes a correct assessment of ad effectiveness of the Apple-Zuties ad type with numerical justification by comparing the percentage of children who chose Choco-Zuties in group B to the corresponding percentage in group C. Section 4 was scored as partially correct. Because three sections were scored as essentially correct and one section was scored as partially correct, the response was initially scored as a 3<sup>1</sup>/<sub>2</sub>.

# AP<sup>®</sup> STATISTICS 2016 SCORING COMMENTARY

## **Question 2 (continued)**

Looking holistically at the response, the absence of any assessment of the Choco-Zuties ad effectiveness in section 4 was viewed as a weakness. Therefore the response earned a score of 3.

### Sample: 2C Score: 2

All three of the required components are present and correct for section 1. The response includes correct null and alternative hypothesis statements for a test of homogeneity and correctly indicates that a chi-square test of homogeneity will be conducted. Note that traditional labels for hypotheses  $H_0$  and  $H_a$  are included in the response but not used to identify the individual hypothesis statements. Correct expected counts (unlabeled) are added to the table in the problem, with unlabeled work shown on the page. The statement "Counted Data greater then [sic] 5: yes" is considered to be referencing the calculated expected counts given its proximity to the work shown. Section 1 was scored as essentially correct. All three of the required components (the value of the chi-square test statistic, the degrees of freedom, and the p-value) are present and correct for section 2, and this section was scored as essentially correct. In section 3 a statement comparing the p-value to the chosen  $\alpha$  level given in the response establishes linkage. The correct decision to reject the null hypothesis is stated. A conclusion is provided in context. However, the choice of wording "the type of ad the children watched affected what snack they choose," suggests that the response refers to the sample data; therefore, it does not satisfy the requirements for a correct conclusion. Because linkage, a correct decision, and context is included in the response, section 3 was scored as partially correct. In section 4 the response refers to the results of the hypothesis test performed in part (a) of the problem, but it does not compare children's snack preference between ad types. Other comments in the response are considered extraneous to the question. Because ad effectiveness is not correctly addressed, section 4 was scored as incorrect. Because two sections were scored as essentially correct, one section was scored as partially correct, and one section was scored as incorrect, the response was initially scored as a 2½. Looking holistically at the paper, the lack of a correct response to part (b), together with weak communication concerning the technical conditions in section 2, was viewed as a weakness. Therefore the response earned a score of 2.